# Enhancing Power Harvesting Using a Tuned Auxiliary Structure

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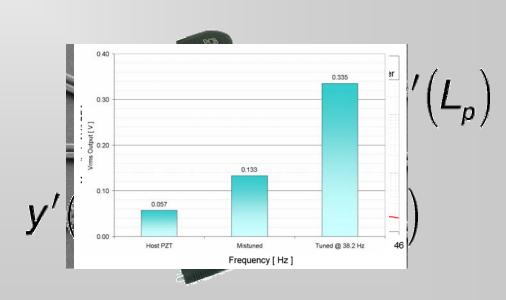
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### Overview

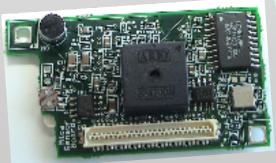
- Motivation
- Theory
- Approach/Experimental Setup
- Tuning Procedure
- Experimental Results
- Conclusions and Recommendations





Energy harvesting is the key to self-sufficient microelectronic devices

- Wireless communications devices
- Digital signal processes
- Wireless sensors
  - Structural health monitoring
  - Damage prognosis



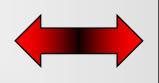




# The Theory because knowing is half the battle

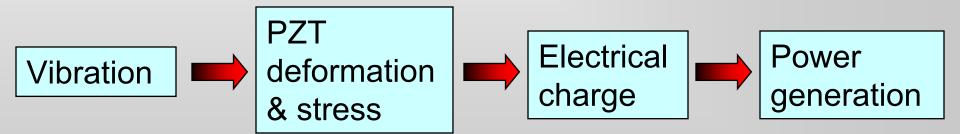
Voltage applied to PZT element:

Its dimension will change



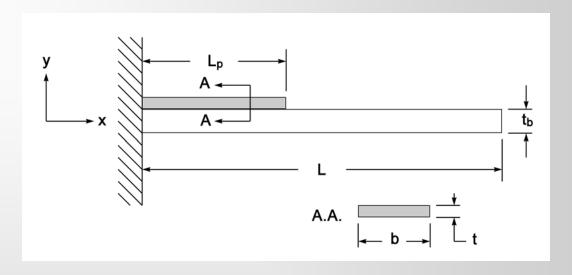
A PZT element is mechanically stressed:

It generates electrical charge





#### Voltage is related to the physical properties of the PZT



$$V_{out}(t) = \frac{q}{C_p} = K_s y'(L_p)$$

$$y'(L_p) =$$
 slope of the auxiliary structure at the end of the PZT patch.



#### The auxiliary structure is tuned to its first bending mode

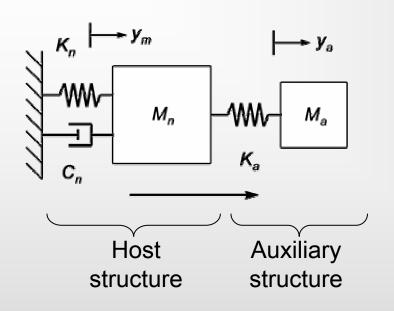
Let's write the slope in terms of tip displacement,

$$y'(x) = \frac{3y_a}{2L^3} \left(2Lx - x^2\right)$$





# The motion of the coupled host structure and PZT can be expressed as a 2-DOF linear system



$$M_a\ddot{y}_a + K_ay_a - K_ay_m = 0$$

$$M_n\ddot{y}_m + C_n\dot{y}_m + K_ny_m - K_ay_a = \phi_{na}\phi_{nk}F$$

Note: we assume negligible damping in the auxiliary structure

$$\begin{bmatrix} Y_{m} \\ Y_{a} \end{bmatrix} = \frac{\begin{bmatrix} K_{a} - M_{a}\omega^{2} & K_{a} \\ K_{a} & K_{n} + K_{a} - M_{n}\omega^{2} + j\omega C_{n} \end{bmatrix}}{\Delta(\omega)} \begin{bmatrix} \phi_{na}\phi_{nk}F(\omega) \\ 0 \end{bmatrix} = \begin{bmatrix} \frac{K_{a} - M_{a}\omega^{2}}{\Delta(\omega)}\phi_{na}\phi_{nk}F(\omega) \\ \frac{K_{a}}{\Delta(\omega)}\phi_{na}\phi_{nk}F(\omega) \end{bmatrix}$$



Assume the auxiliary structure is perfectly tuned to its host structure:

$$V_{a} = \frac{-\phi_{na}\phi_{nk}F}{K_{a}} = \frac{-\phi_{na}\phi_{nk}FL^{3}}{3EI}$$

$$V'(x) = \frac{3y_{a}}{2L^{3}}(2Lx - x^{2})$$

$$V_{out}(t) = \frac{q}{C_{p}} = K_{s}y'(L_{p})$$

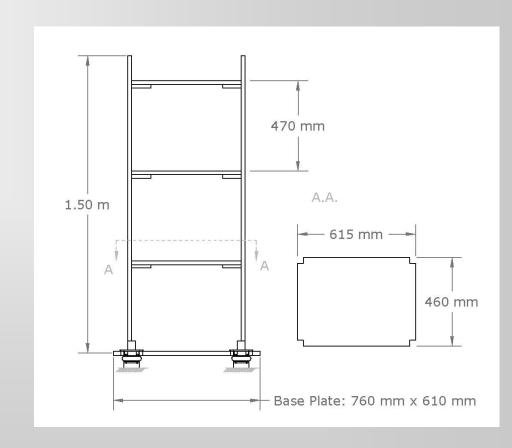
$$V_{out}(t) = \frac{K_s \phi_{na} \phi_{nk} F}{2EI} \left( 2LL_p - L_p^2 \right)$$



### Approach/Experimental Setup What are we harvesting energy from??



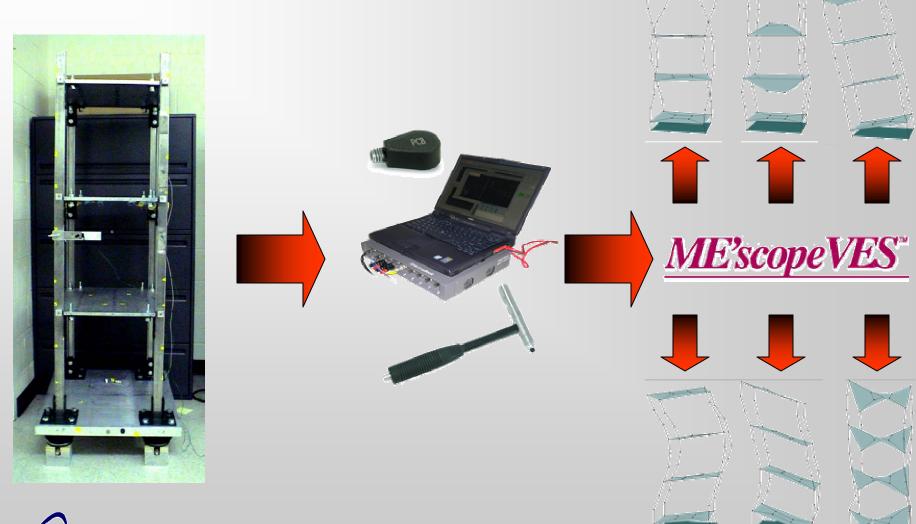






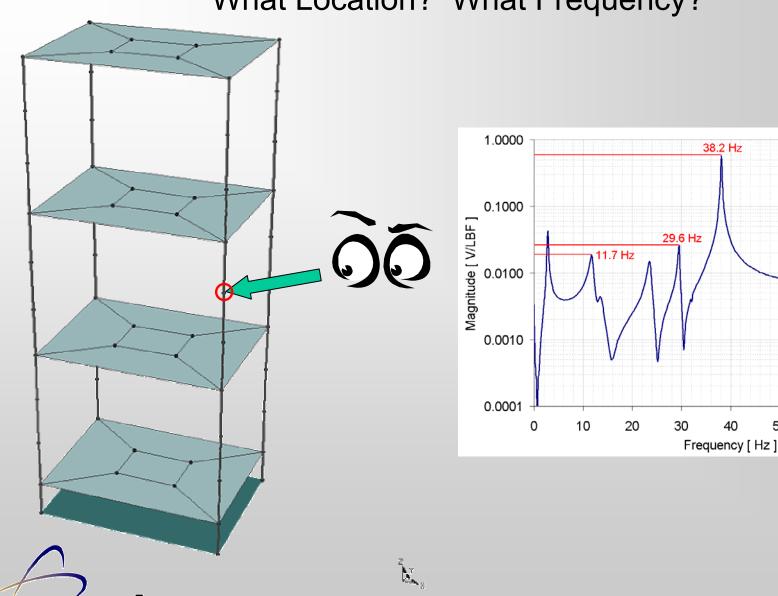
#### **Experimental Setup**

Learning the dynamic characteristics of our host structure



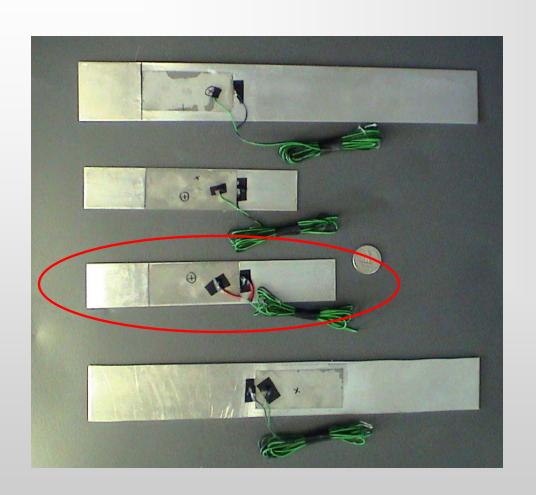


### The Tuning Procedure What Location? What Frequency?



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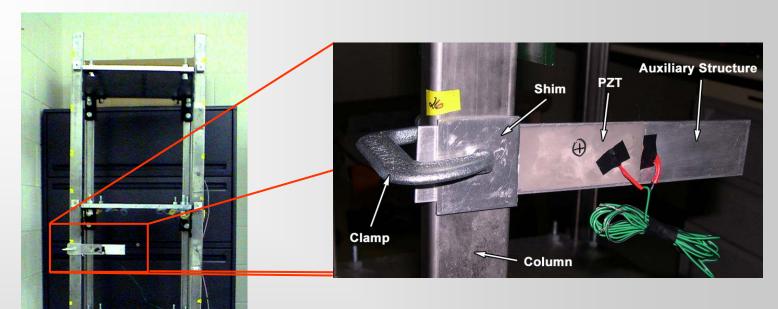
#### Sample auxiliary structures



$$f_1 = \frac{1}{2\pi} \sqrt{\frac{3EI}{L^3 (M + 0.24M_b)}}$$



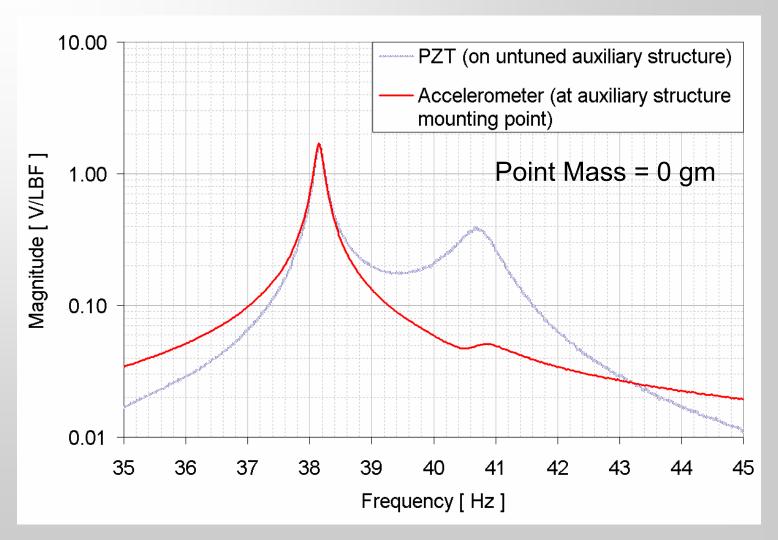
#### Mounting the Auxiliary Structure...







#### Iteration #1





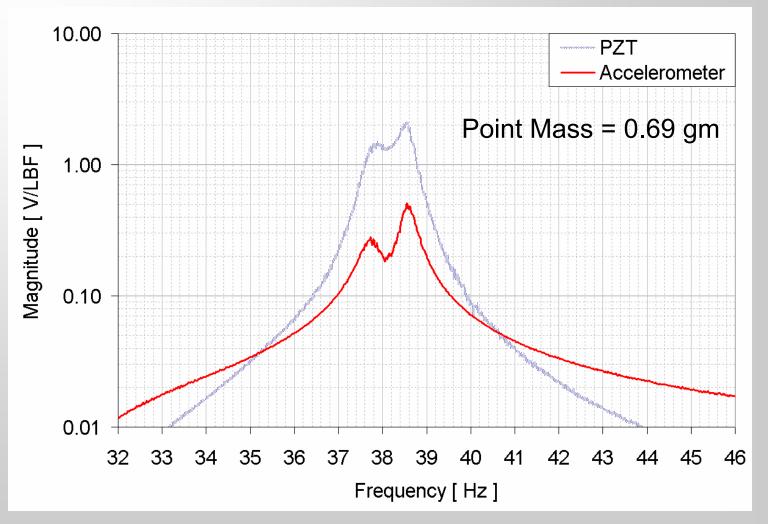
В





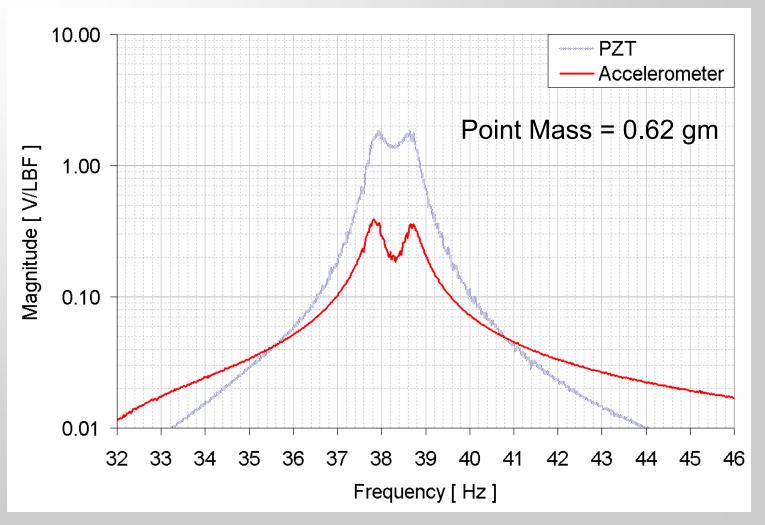


#### Iteration #3



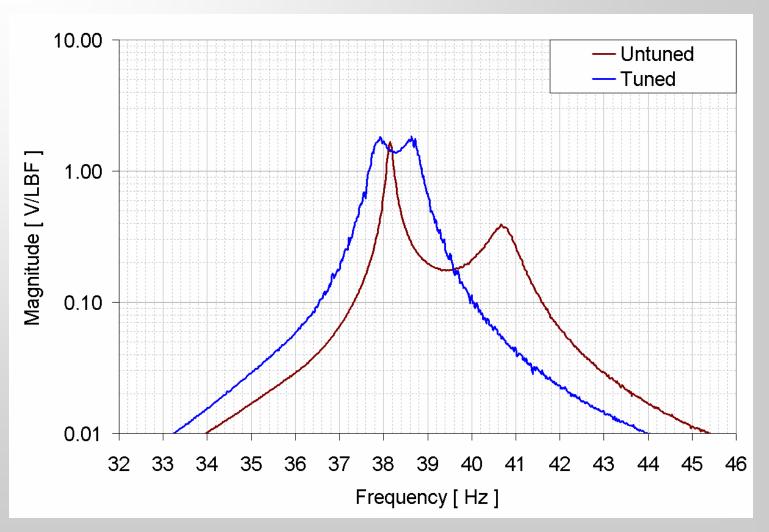


#### Iteration #5



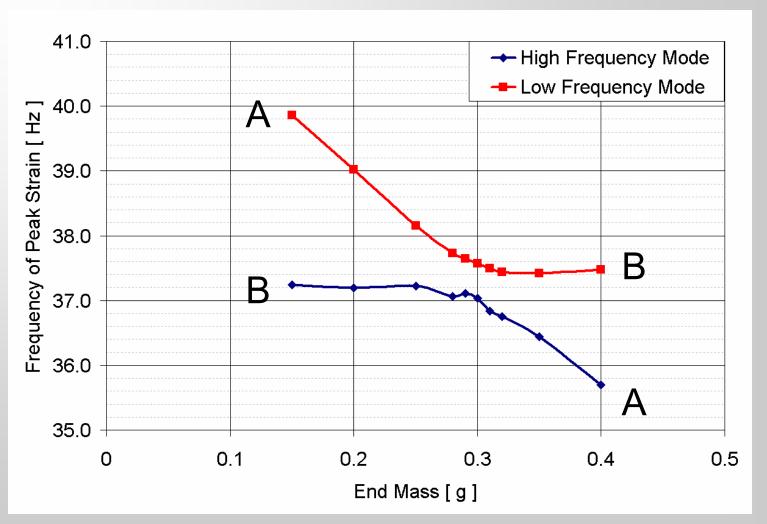


#### **Tuned and Mistuned PZT FRFs**



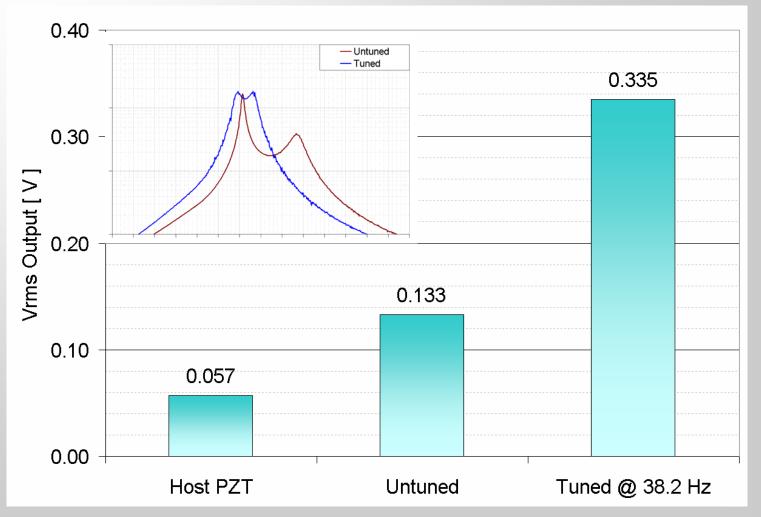


#### FRF peaks do NOT merge



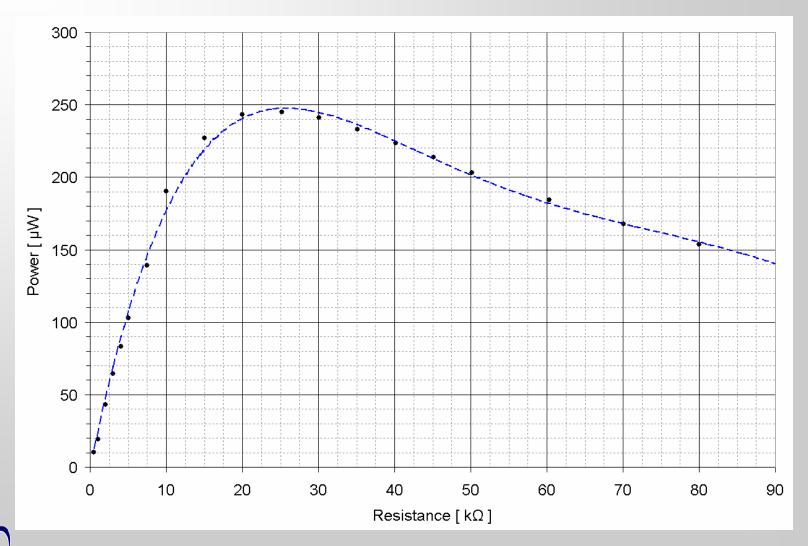


## A tuned auxiliary structure demonstrates increased open-loop voltage output



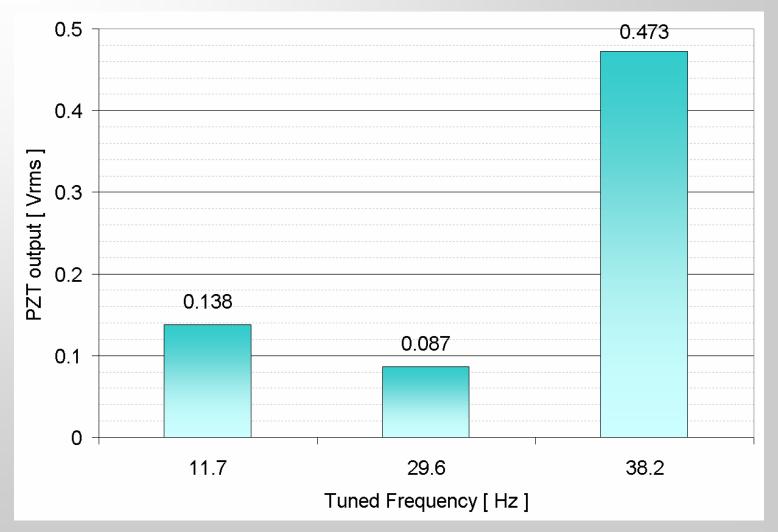


#### Impedance-matching shows optimal PZT loading



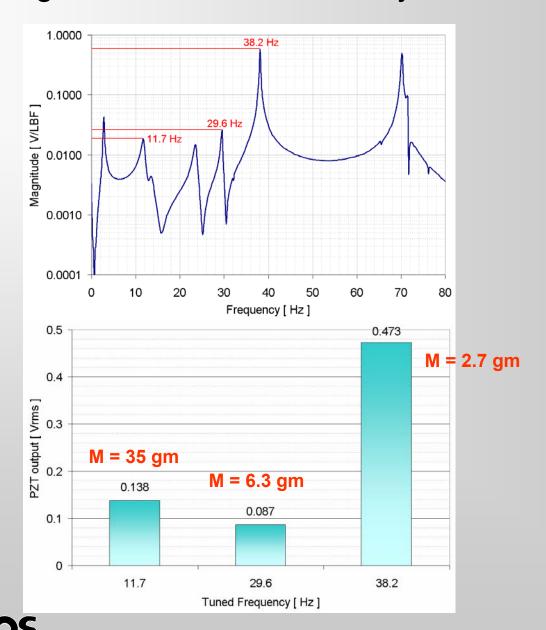


#### FRFs of large magnitudes increase auxiliary structure efficiency





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# Enhanced power harvesting can be achieved using a tuned auxiliary structure

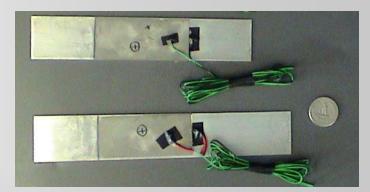
- Even mistuned auxiliary structures are beneficial
- Important parameters
  - Magnitude of mode shape at auxiliary structure's location
- Considerations for other applications
  - Time invariance
  - Input force characteristics
  - Auxiliary structure geometric constraints



### Recommendations

- Single variable analysis of auxiliary structures
  - Length
  - Thickness
- PZT patch size
- Multiple PZT patches
  - In parallel (increase current)
  - In series (increase voltage output)
- Circuit optimization

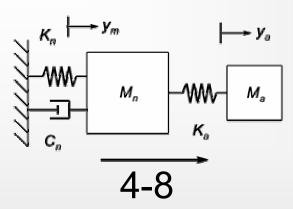




### Acknowledgements

- Vibrant Technologies
  - MEScopeVES experimental modal analysis software
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  - MATLAB numerical analysis software
- Hibbitt, Karlsson and Sorensen, Inc.
  - ABAQUS finite element software

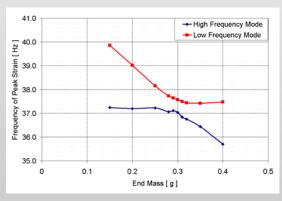




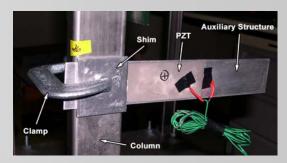


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### Questions?







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